

Surveys in Differential Geometry

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Volume II

Surveys in
Differential Geometry

Proceedings of the conference
on geometry and topology
held at Harvard University
April 23-25, 1993

edited by
C.C. Hsiung and S.-T. Yau

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Preface

In 1993, the *Journal of Differential Geometry* sponsored another conference on differential geometry. The first conference of this type was held in 1990. The proceedings were published in 1991 in *Surveys in Differential Geometry, 1991*. There is still significant interest in this volume and there continues to be developments in the subject. For this reason, we intend on sponsoring this conference and the accompanying publication once every three years.

The conference was held at Harvard University, coinciding with a celebration of Raoul Bott's 70th birthday. We are very grateful to the speakers, who attracted a large audience, and to the more than three hundred participants, whose participation made this conference a success.

We wish to thank Harvard University Mathematics department for supporting the conference, especially Wilfried Schmid who was then the Department Chair, Ruby Aguirre, the department administrator, and to the editors of the *Journal of Differential Geometry*, whose continued support of the journal make it the successful publication that it is.

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